Séminaire d'algèbre, topologie et géométrie Jeudi 6 juin à 11h Salle I

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Bousfield localization and commutative monoids

We give conditions on a monoidal model category M and on a set of maps S so that the Bousfield localization of M with respect to S preserves strict commutative monoids. This problem was motivated by an example due to Mike Hill which demonstrates that for the model category of equivariant spectra, even very nice localizations can fail to preserve strict commutative monoids. A recent theorem of Hill and Hopkins gives conditions on the localization to prohibit this behavior. When we specialize our general machinery to the model category of equivariant spectra we recover this theorem.

En route to solving the localization problem we will introduce the Σ_n equivariant monoid axiom, which guarantees us that commutative monoids
inherit a model structure. This axiom has a nice generalization which gives
model structures and semi-model structures on algebras over an operad for
various classes of operads. If there is time we will discuss this and say a word
about how it interacts with Bousfield localization.