

# Artificial Neural Networks in financial applications

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Michel Verleysen

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- /// Artificial neural networks
  - /// Introduction
  - /// Multi-Layer Perceptron
  - /// Radial-Basis Function Networks
  - /// Self-Organizing Maps
- /// About the choice of parameters
  - /// # of units or parameters
  - /// # of inputs
- /// Two application examples in finance
  - /// Time series forecasting
  - /// Classification of investment funds



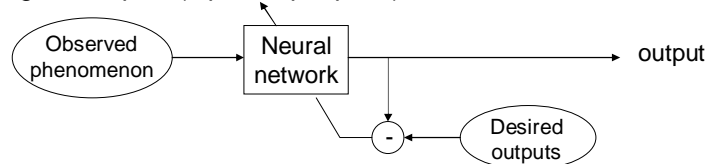
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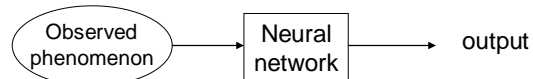


## Learning in ANN

- /// Supervised learning: building an input-output relation known through examples (input-output pairs)



- /// Unsupervised learning: modeling a property of the input data (for example density)



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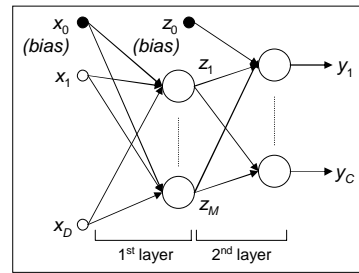


## Multi-layer perceptron (MLP)

$$y_k(\mathbf{x}) = h\left(\sum_{j=0}^M w_{kj}^{(2)} g\left(\sum_{i=0}^D w_{ji}^{(1)} x_i\right)\right)$$

$$\mathbf{y}(\mathbf{x}) = \mathbf{h}(\mathbf{w}^{(2)} \mathbf{g}(\mathbf{w}^{(1)} \mathbf{x}))$$

parameters



- ⚡ Convention: 2 layers of weights (in literature: sometimes 3 layers of *units* or *neurons*)
- ⚡  $g$  and  $h$  continuous, bounded, non-linear functions (tanh, sigmoid)
- ⚡  $h$  can be linear but not  $g$  (otherwise only one layer)



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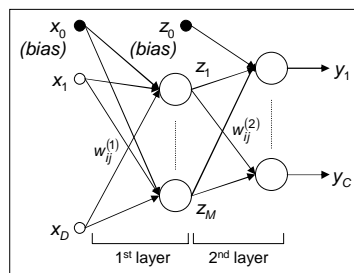
## Learning in MLP

- ⚡ Learning =
  - ⚡ definition of an error criterion  $E$
  - ⚡ evaluation of derivatives of  $E$  w.r.t. parameters  $w$
  - ⚡ adjustments of parameters  $w$  according to derivatives

- ⚡ Error criterion (for one output):

$$E = \sum_{p=1}^P \|y^p - d^p\|^2$$

Training examples



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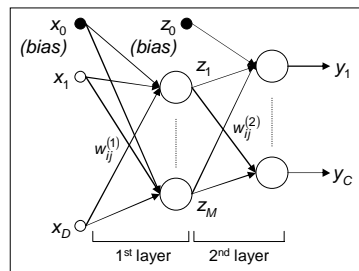
## Learning in MLP

⚡ “Back-propagation”:  $\frac{\partial E}{\partial w_{ij}}$

⚡ For last layer  $w_{ij}^{(2)}$ : easy

⚡ For other layers: computed according to derivatives of *next* layer

→ *back-propagation* of derivatives



⚡ More elaborated learning methods:

- ⚡ Conjugate gradients
- ⚡ Levenberg-Marquardt
- ⚡ ...



## Universal approximation property

⚡ “A 2-layer MLP can approximate arbitrarily well any (functional) continuous mapping, provided the number  $M$  of hidden units is sufficiently large”

⚡ But:

- ⚡ what about generalization?
- ⚡ what about the number  $M$  of hidden units?
- ⚡ What about initialization and local minima?
- ⚡ Learning is slow, difficult, needs expertise, etc.



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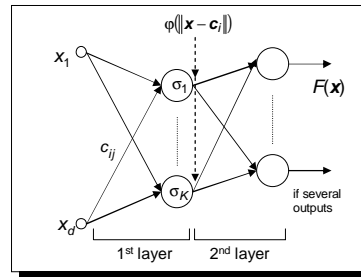
# Radial-Basis Function Networks (RBFN)

$$F(\mathbf{x}) = \sum_{i=1}^K w_i \phi(\|\mathbf{x} - \mathbf{c}_i\|)$$

$$\phi(\|\mathbf{x} - \mathbf{c}_i\|) = \exp\left(-\frac{\|\mathbf{x} - \mathbf{c}_i\|^2}{2\sigma_i^2}\right)$$

⚡ Recommended:

$$F(\mathbf{x}) = \sum_{i=1}^K w_i \exp\left(-\frac{\|\mathbf{x} - \mathbf{c}_i\|^2}{2\sigma_i^2}\right) + \sum_{i=1}^D w'_i x_i + w'_0$$



- ⚡ RBFN are a generalization of the
  - ⚡ interpolation problem
  - ⚡ regularization problem

because  $K \ll P$



## RBFN: learning strategies

$$F(\mathbf{x}) = \sum_{i=1}^K w_i \varphi(\|\mathbf{x} - \mathbf{c}_i\|) \quad \varphi(\|\mathbf{x} - \mathbf{c}_i\|) = \exp\left(-\frac{\|\mathbf{x} - \mathbf{c}_i\|^2}{2\sigma_i^2}\right)$$

- ⚡ Parameters to be determined:  $\mathbf{c}_i$ ,  $\sigma_i$ ,  $w_i$
- ⚡ Traditional learning strategy: splitted computation
  1. centers  $\mathbf{c}_i$
  2. widths  $\sigma_i$
  3. weights  $w_i$



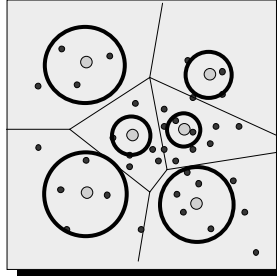
## RBFN: computation of centers

- ⚡ Idea: centers  $\mathbf{c}_i$  must have the (density) properties of learning points  $\mathbf{x}^k$ 
  - vector quantization
    - ⚡ selected at random (in learning set)
    - ⚡ competitive learning
    - ⚡ frequency-sensitive learning
    - ⚡ Kohonen maps
- ⚡ This phase only uses the  $\mathbf{x}^k$  information, not the  $t^k$



## RBFN: computation of widths

- ⚡ Universal approximation property: valid with identical widths
- ⚡ In practice (limited learning set): variable widths  $\sigma_i$
- ⚡ Idea: RBFN use *local* clusters



- ⚡ choose  $\sigma_i$  according to standard deviation of clusters



## RBFN: computation of weights

$$F(\mathbf{x}) = \sum_{i=1}^K w_i \varphi(\|\mathbf{x} - \mathbf{c}_i\|) \quad \varphi(\|\mathbf{x} - \mathbf{c}_i\|) = \exp\left(-\frac{\|\mathbf{x} - \mathbf{c}_i\|^2}{2\sigma_i^2}\right)$$

constants !

- ⚡ Problem becomes linear !
- ⚡ Solution of least square criterion  $E(F) = \frac{1}{2P} \sum_{p=1}^P (t^p - F(\mathbf{x}^p))^2$  leads to

$$\mathbf{w} = \Phi^+ \mathbf{t} = (\Phi^T \Phi)^{-1} \Phi^T \mathbf{t}$$

where

$$\Phi \equiv \varphi_{ki} = \varphi(\|\mathbf{x}^k - \mathbf{c}_i\|)$$

- ⚡ In practise: use SVD !



## RBFN: gradient descent

$$F(\mathbf{x}) = \sum_{i=1}^K w_i \exp\left(-\frac{\|\mathbf{x} - \mathbf{c}_i\|^2}{2\sigma_i^2}\right)$$

Diagram illustrating the components of the RBFN function  $F(\mathbf{x})$ :

- 1: The entire function  $F(\mathbf{x})$  is supervised.
- 2: The Gaussian kernel  $\exp\left(-\frac{\|\mathbf{x} - \mathbf{c}_i\|^2}{2\sigma_i^2}\right)$  is unsupervised.
- 3: The weights  $w_i$  are supervised.

∴ 3-steps method: supervised unsupervised

- ∴ Once  $\mathbf{c}_i, \sigma_i, w_i$  have been set by the previous method, possibility of gradient descent on *all* parameters
- ∴ Some improvement, but
  - ∴ learning speed
  - ∴ local minima
  - ∴ risk of non-local basis functions
  - ∴ etc.



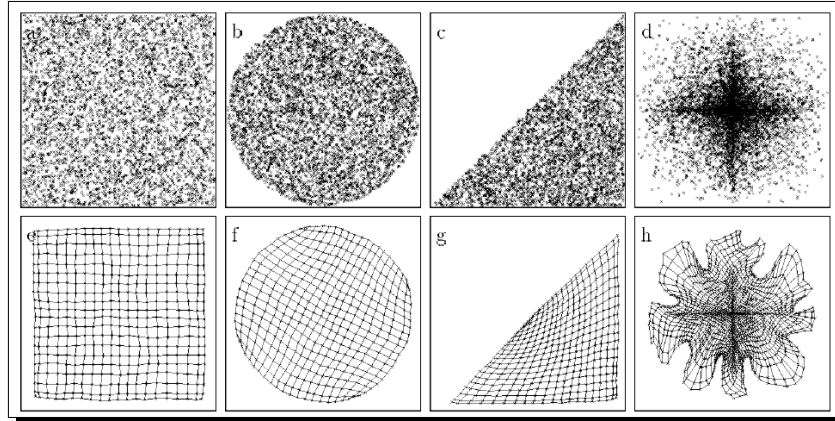
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## Examples after convergence



2-dimensional input spaces!



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## SOM equations

⚡ Choice of the winner

$$y_k = \max_i (f(\mathbf{w}_i^T \mathbf{x}))$$

⚡ Adaptation of weights

$$\mathbf{w}_j(t+1) = \begin{cases} \mathbf{w}_j(t) + \alpha(t)(\mathbf{x} - \mathbf{w}_j(t)) & \text{if } d(k, j) < r(t) \\ \mathbf{w}_j(t) & \text{otherwise} \end{cases}$$

⚡  $r(t)$  is made decreasing with time

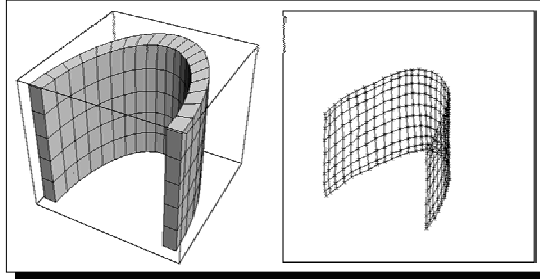


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# SOM used as data analysis tool

Mapping (projection) of a continuous distribution to a discrete set (the centroids)



After learning: nearest neighbour rule in the input space



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# Macroeconomical data (1/2)

Factors: annual increase (%), infant mortality (‰), illiteracy ratio (%), school attendance (%), GIP, annual GIP increase (%)

Afrique du sud	2.9	89.0	50.0	19.0	2680.0	-2.9	Italie	0.4	13.0	4.6	73.0	6869.0	-1.2
Algerie	2.9	114.0	58.5	47.9	2266.0	0.1	Japon	0.9	6.6	0.8	92.0	9704.0	3.0
Arabie Saoudite	4.2	111.0	75.4	39.7	10827.0	-10.8	Kenya	4.0	85.0	52.9	59.3	376.0	3.6
Argentine	1.2	44.0	5.3	69.5	2264.0	2.0	Koweit	6.5	33.0	35.9	73.0	20900.0	-0.5
Australie	1.3	10.4	0.0	86.0	9938.0	-1.2	Madagascar	2.7	69.0	38.8	30.4	259.0	0.9
Bahrein	3.8	57.0	20.9	76.3	8960.0	-10.1	Maroc	2.5	104.0	65.0	34.9	864.0	0.6
Bresil	2.2	75.0	23.9	62.3	1853.0	-3.9	Mali	2.8	152.0	86.5	16.7	190.0	1.5
Cameroun	2.4	106.0	55.1	44.5	939.0	6.5	Mexique	2.6	54.0	17.3	70.1	1900.0	-4.6
Canada	1.0	10.0	0.9	93.0	9857.0	3.0	Mozambique	2.7	150.0	66.8	16.1	155.0	-6.9
Chili	1.7	42.0	7.7	85.2	1853.0	-0.5	Nicaragua	4.4	88.0	10.0	52.5	760.0	5.1
Chine	1.4	71.0	31.0	44.0	231.0	10.0	Niger	3.0	143.0	90.2	9.2	330.0	2.5
Coree du Sud	1.6	33.0	8.3	82.1	1716.0	9.3	Nigeria	3.3	133.0	66.0	29.3	807.0	-4.0
Cuba	0.7	16.8	8.9	78.7	2046.0	5.2	Perou	2.8	85.0	19.3	72.0	997.0	-12.0
Egypte	2.7	74.0	58.1	45.8	626.0	6.0	Pologne	0.9	24.6	0.6	77.0	2545.0	4.5
Espagne	0.9	9.6	6.8	88.0	5316.0	2.3	RDA	-0.2	11.4	0.5	89.0	5103.0	4.2
Etats Unis	1.0	11.2	0.8	91.0	11732.0	3.3	RFA	-0.1	12.0	0.7	87.0	12176.0	1.0
Ethiopie	2.7	145.0	85.0	23.1	140.0	7.4	Royaume Uni	-0.1	10.1	0.8	83.0	8655.0	3.5
Finlande	0.6	6.5	0.6	98.0	10286.0	5.1	Sénégal	2.6	152.0	77.5	19.2	430.0	2.3
France	0.4	9.1	1.2	86.0	11326.0	0.5	Suede	0.1	7.0	0.6	85.0	13920.0	1.8
Grece	1.1	15.1	11.7	81.0	4060.0	0.3	Suisse	0.6	8.0	0.9	88.0	15522.0	-0.1
Haute Volta	1.7	208.0	88.6	7.6	240.0	3.6	Syrie	3.8	60.0	46.3	50.7	1717.0	5.8
Hongrie	0.0	20.0	0.9	42.0	1963.0	0.9	Turquie	2.1	119.0	31.2	42.0	1491.0	3.0
Inde	1.8	121.0	57.6	71.7	260.0	6.5	URSS	0.9	28.8	0.8	96.0	4562.0	4.0
Indonesie	1.7	99.0	32.3	41.3	488.0	5.0	Venezuela	3.0	40.0	19.0	57.7	3823.0	-2.0
Iran	2.7	105.0	57.2	57.9	2346.0	5.2	Vietnam	2.3	97.0	13.0	59.5	220.0	5.2
Irlande	1.2	11.0	1.0	93.0	4813.0	0.5	Yougoslavie	0.9	31.0	13.2	83.0	2067.0	-1.3
Israel	2.2	15.0	6.7	74.0	4531.0	1.1							

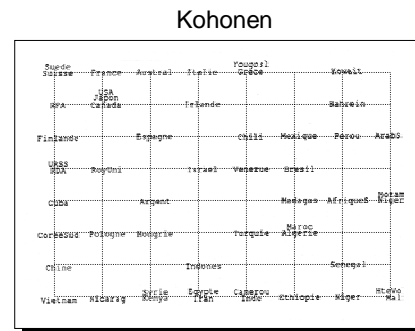
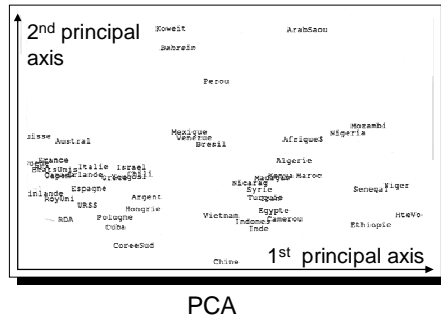


From "Data analysis: How to compare Kohonen neural networks to other techniques?", F. Blayo, P. Demartines, in IWANN91 (Granada, Spain) proceedings, Springer-Verlag Lecture Notes in Computer Sciences 540, pp. 469-476.

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## Macroeconomical data (2/2)



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## # of units or parameters in ANN

- ⚡ # units: illustration of bias-variance dilemma
  - ⚡ # units increases: better learning, overfitting ↗
  - ⚡ # units decreases: poorest learning, overfitting ↘
- ⚡ A posteriori test with ≠ numbers of units/parameters!
- ⚡ Aim: optimal generalization error

$$E_{gen}(\theta) = \lim_{T \rightarrow \infty} \sum_{t=1}^T \frac{(g(x_t, \theta) - y_t)^2}{T} \longrightarrow \hat{E}_{gen}(\theta)$$



## Estimation of generalization error

$$E_{gen}(\theta) = \lim_{T \rightarrow \infty} \sum_{t=1}^T \frac{(g(x_t, \theta) - y_t)^2}{T} \longrightarrow \hat{E}_{gen}(\theta)$$

- ⚡ Estimates of generalization error:
  - ⚡ (k-fold) cross-validation
  - ⚡ leave-one-out
  - ⚡ bootstrap
- ⚡ General principle: use different samples to
  - ⚡ learn
  - ⚡ validate (compare and select models)
  - ⚡ test (assess the performances)



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# # of inputs in ANN

- /// Learning in high-dimensional spaces:
  - number of samples  $\approx e^{\text{space dimension}}$
- /// → necessity to *reduce* the input space dimension!
  
- /// How?
  - /// Selection of input variables
    - /// Test and errors (comparison of models)
  - /// Projection of input variables
    - /// Principal Component Analysis
    - /// Curvilinear Component Analysis
  
- /// How much?
  - /// A posteriori measures (idem model selection)
  - /// Specific methods (ex: time series)



## Input variables selection and projection

- ⚡ Starting with many input variables, then reduce their number
- ⚡ Two options:
  1. selection of input variables
    - ↗ interpretability
    - ↘ limited to existing variables
  2. projection of input variables
    - ⚡ linear: PCA
    - ⚡ non-linear: CCA, Kohonen, etc.  
forecasting: based on **Taken's theorem**



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## Application of dimension reduction to forecasting tasks

- ⚡ Regressor: - past values  $x(t-i)$
- exogenous data  $in(j)$

- ⚡ Forecasting

$$x(t+1) = f(x(t), x(t-1), \dots, x(t-k), in(1), in(2), \dots, in(l))$$

- ⚡ Non-linear forecasting:

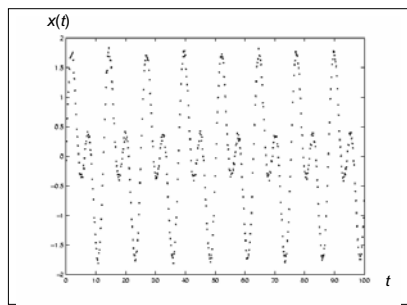
- ⚡ 1. optimise regressor on linear predictor
- ⚡ 2. use the same regressor with non-linear predictor  $f$
- ⚡ trials and errors (computational load !)
- ⚡ (non-linear) projection of regressor variables



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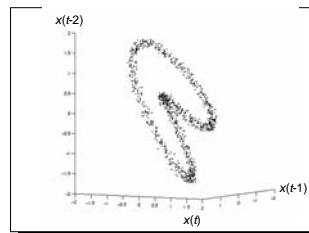
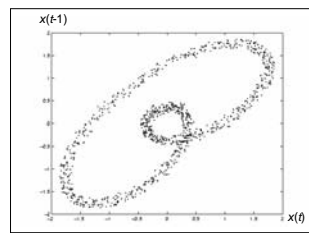
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## Forecasting: Taken's theorem 1/2



time series

intrinsic dimension ( $q$ ) = 1



- ⚡ Takens' theorem:

$$q \leq \text{size of regressor} \leq 2q+1$$

(AR model)



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## Forecasting: Taken's theorem 2/2

- ⚡ Takens' theorem:  
 $q \leq \text{size of regressor} \leq 2q+1$
- ⚡ In the  $2q+1$  space, there exists a  $q$ -surface without intersection points
- ⚡ Projection from  $2q+1$  to  $q$  possible !



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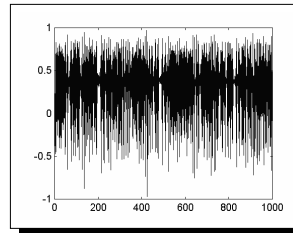
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## Forecasting: 1st example 1/2

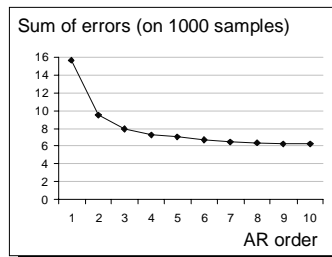
- ⚡ Artificial series

$$x(t+1) = ax(t)^2 + bx(t-2) + \varepsilon(t)$$

Two past values!



- ⚡ Linear AR model

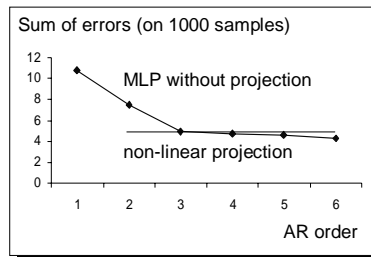


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## Forecasting: 1st example 2/2

- ⚡ Non-linear AR model
  - ⚡ initial regressor: size=6
  - ⚡ intrinsic dimension: 2
  - ⚡ CCA from dim=6 to dim=2
  - ⚡ MLP on 2-dim data

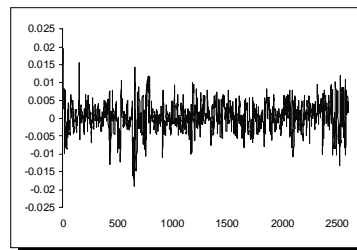


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## Forecasting: 2nd example 1/2

- ⚡ Daily returns of BEL20 index



- ⚡ 42 indicators from inputs and exogenous variables:
  - ⚡ returns:  $X_t, X_{t-10}, X_{t-20}, X_{t-40}, \dots, Y_t, Y_{t-10}, \dots$
  - ⚡ differences of returns:  $X_t - X_{t-5}, X_{t-5} - X_{t-10}, \dots, Y_t - Y_{t-5}$
  - ⚡ oscillators:  $K(20), K(40), \dots$
  - ⚡ moving averages:  $MM(10), MM(50), \dots$
  - ⚡ exponential moving averages:  $MME(10), MME(50), \dots$
  - ⚡ etc



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## Forecasting: 2nd example 2/2

### Method:

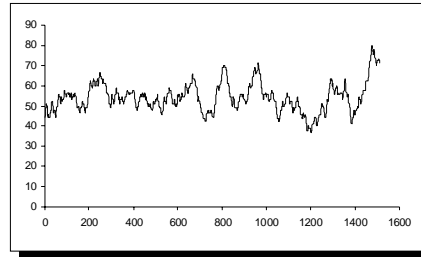
- 42 indicators
- PCA → 25 variables

Grassberger-Proccacia: intrinsic dimension = 9

- CCA → 9 variables
- RBF → forecasting

### Result: % of correct approximations of sign (90-days average)

- In average: 57.2% on test set

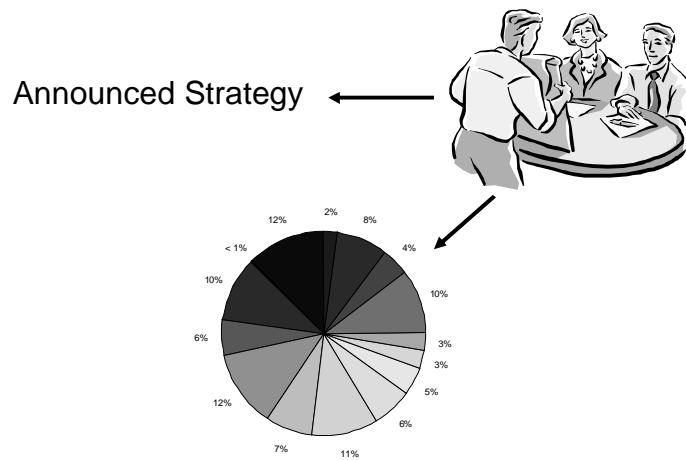


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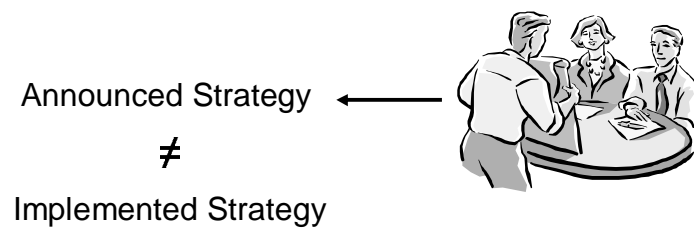
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## Why This Study ?



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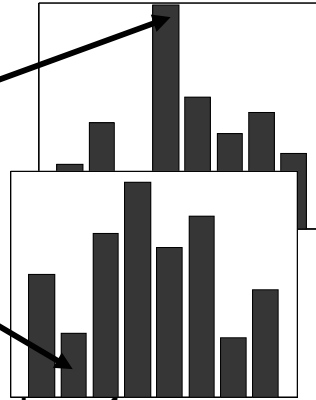
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## Why This Study ?

Announced Strategy

≠

Implemented Strategy



Goal of managers:

To be compared to other ones with weaker performances

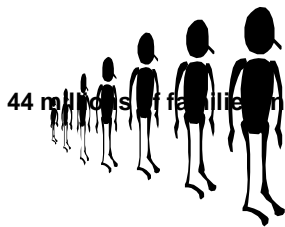


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## Why This Study ?

44 millions of families in USA



Not able to estimate the real risk

Classifications exist  
They are not very good

Kim T.-H., Stone D. and Tomas M., *Mutual fund objective misclassification*. Journal of Economics and Business, 2000. **52**: p. 309-323.



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## Extraction of Features Linear Regression

$$R_i(t) = b_{1i}F_1(t) + b_{2i}F_2(t) + \dots + b_{ni}F_n(t) + e_i(t)$$

↓  
Return of a fund

↓  
Index Return

$b_{ij}$  determined using a Least-Square method



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## Extraction of Features Linear Regression under constraints

$$R_i(t) = b_{1i}F_1(t) + b_{2i}F_2(t) + \dots + b_{ni}F_n(t) + e_i(t)$$

$$\sum_j b_{ij} = 1$$

$b_{ij}$  percentages of investment

$$b_{ij} \geq 0, \forall i, j$$



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## Extraction of Features Multi-collinearity problem and PCA

$$R_i(t) = b_{1i}F_1(t) + b_{2i}F_2(t) + \dots + b_{ni}F_n(t) + e_i(t)$$

Not equal, but highly correlated  
 $b_{ji}$  are difficult to determine



## Extraction of Features Multi-collinearity problem and PCA

$$R_i(t) = b_{1i}F_1(t) + b_{2i}F_2(t) + \dots + b_{ni}F_n(t) + e_i(t)$$

$$F_1, F_2, \dots, F_n \xrightarrow{\text{PCA}} G_1, G_2, \dots, G_m$$

$$R_i(t) = c_{1i}G_1(t) + c_{2i}G_2(t) + \dots + c_{mi}G_m(t) + e_i(t)$$

$$G_1, G_2, \dots, G_m \xrightarrow{\text{Inverse of PCA}} F_1, F_2, \dots, F_n$$

$$R_i(t) = b'_{1i}F_1(t) + b'_{2i}F_2(t) + \dots + b'_{ni}F_n(t) + e_i(t)$$



## Classification of investment funds

- ⚡ Extraction of features
  - ⚡ Linear Regression (under constraints)
  - ⚡ *Multi-collinearity* problem and PCA
- ⚡ Classification
  - ⚡ Kohonen Maps
  - ⚡ Ward algorithm
- ⚡ Application
  - ⚡ CRSP database (the Chicago University)
  - ⚡ Comparison with classification from the ICDI and S&P's Fund Services.



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## CRSP database (the Chicago University)

	indexes
1	Dow Jones 30
2	Lehman Brothers' US Credit Bond Index
8	Salomon Brothers' Non-US Government Bond Index
9	S&P400 Medium Capitalization
14	FTSE100
17	FTSE Small Capitalization
18	UK Bank Bills 3 month
21	TOPIX100
24	Japan Benchmark 2 year Government Index
26	CAC40
29	France Benchmark 2 year Government
32	Germany Money Market 3 month

**5822 funds**

**33 indexes**



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## CRSP database (the Chicago University)

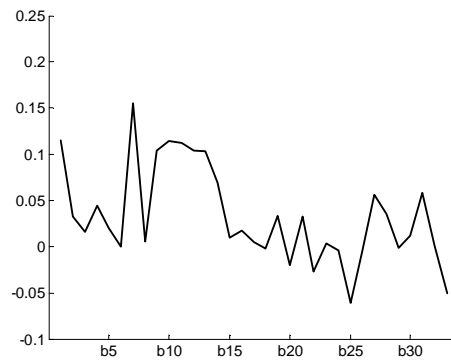
	indexes	$b'_i$
1	Dow Jones 30	0.1156
2	Lehman Brothers' US Credit Bond Index	0.0322
8	Salomon Brothers' Non-US Government Bond Index	0.0055
9	S&P400 Medium Capitalization	0.1042
14	FTSE100	0.6090
17	FTSE Small Capitalization	0.0044
18	UK Bank Bills 3 month	0.0336
21	TOPIX100	0.0326
24	Japan Benchmark 2 year Government Index	-0.0048
26	CAC40	-0.0057
29	France Benchmark 2 year Government	-0.0012
32	Germany Money Market 3 month	0.0016



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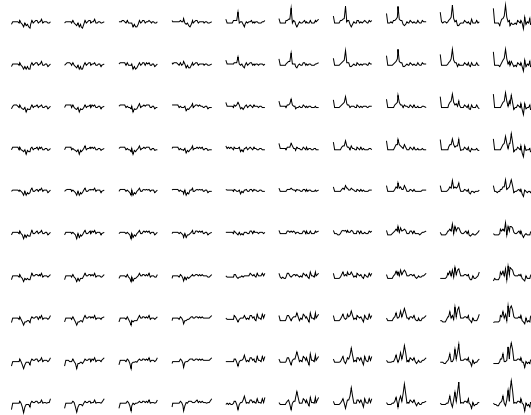
## CRSP database (the Chicago University)



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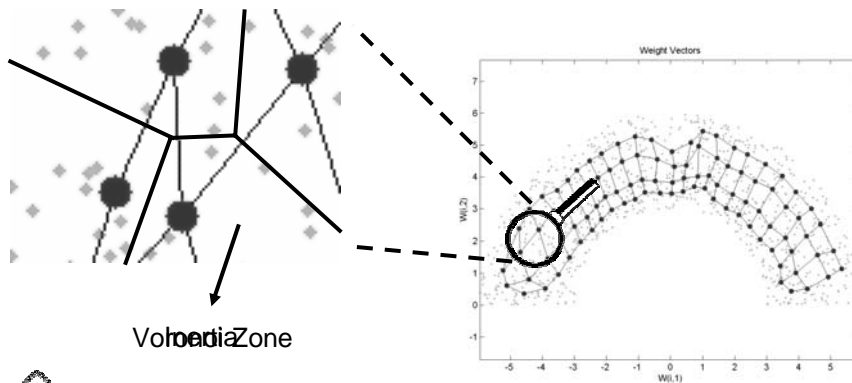
# CRSP database Kohonen



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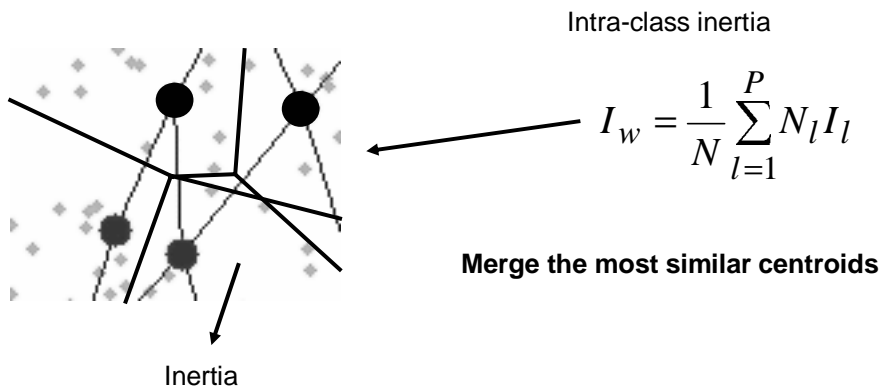
# Classification Ward Algorithm



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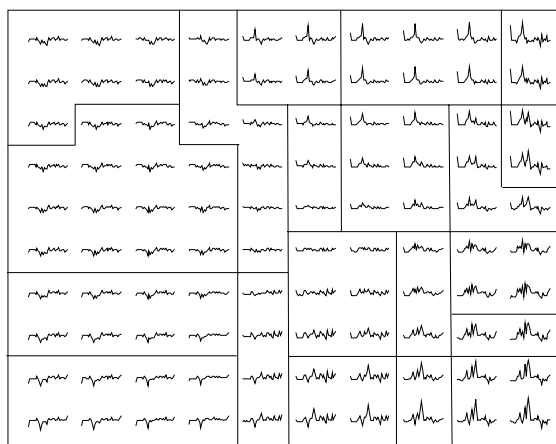
# Classification Ward Algorithm



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# CRSP database Ward: 20 classes



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## Comparison to classification from the ICDI and S&P's Fund Services.

Strategies		
Aggressive Growth	Government Securities	Taxable Money Market
Balanced	International Equities	High Quality Municipal Bonds
High Quality Bonds	Income	Option Income
High Yield Bonds	Long-Term Growth	Precious Metals
Global Bonds	Tax-Free Money Market	Sector Funds
Global Equity	Gov Securities Money Market	Special Funds
Growth & Income	High Quality Municipal Bonds	Total Return
Ginnie Mae Funds	Single-State Municipal Bonds	Utility Funds



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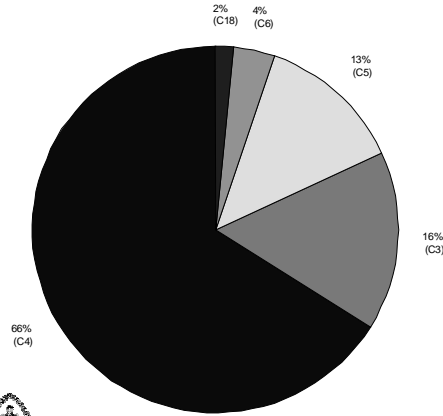


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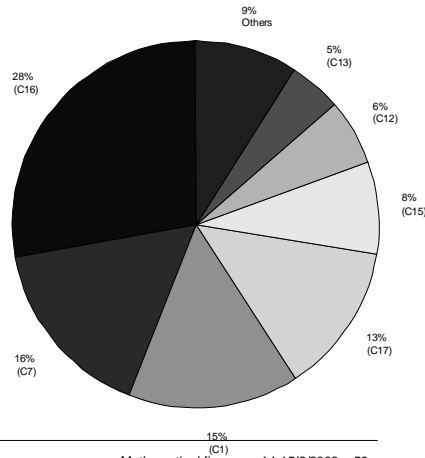
## Comparison to classification from the ICDI and S&P's Fund Services.

**SINGLE-STATE MUNICIPAL BOND FUNDS**



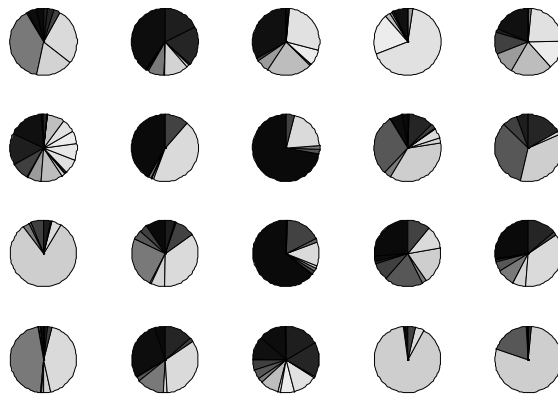
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**LONG-TERM GROWTH FUNDS**



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## Comparison to classification from the ICDI and S&P's Fund Services.



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# Analysis

Intra-class inertia for classifications:

- 0.07 for the Kohonen/Ward classification
- 0.13 for the reference classification

Why some differences between the two classifications ?

- classification from ICDI based on information given by the managers ?
- reference classification not so sophisticated ?
- strategy not constant ?



# Conclusion

- /// ANN are regression/classification tools:
  - /// powerful in theory
  - /// powerful in practice
  - /// but application needs caution and expertise:
    - /// choosing # of parameters
    - /// choosing # and which inputs
    - /// learning procedure (local minima, etc.)
    - /// validation !
    - /// comparison with more classical tools
    - /// etc.

